

# Machine Learning in Search

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# Motivation & Overview



## Digital revolution

- Digital revolution: **production, storage & accessibility** of knowledge.
- Digital collections replace libraries, digital content creation, online publication
- Increase in comprehensiveness, freshness, distribution, accessibility, usability, applications



WORLD INTERNET USAGE AND POPULATION STATISTICS						
World Regions	Population (2009 Est.)	Internet Users Dec. 31, 2008	Internet Users Latest Data	Penetration (% Population)	Growth 2008-2009	Users % of Table
Africa	991,002,342	4,514,400	65,903,900	6.7 %	1,359.9 %	3.9 %
Asia	3,808,070,503	114,304,000	704,213,930	18.5 %	516.1 %	42.2 %
Europe	803,850,858	105,096,093	402,380,474	50.1 %	282.9 %	24.2 %
Middle East	202,687,005	3,284,800	47,964,146	23.7 %	1,360.2 %	2.9 %
North America	340,831,831	108,096,800	251,735,500	73.9 %	132.9 %	15.1 %
Latin America/Caribbean	586,662,468	18,068,919	175,834,439	30.0 %	873.1 %	10.5 %
Oceania / Australia	34,700,201	7,620,480	20,838,019	60.1 %	173.4 %	1.2 %
<b>WORLD TOTAL</b>	<b>6,767,805,208</b>	<b>360,985,492</b>	<b>1,668,870,408</b>	<b>24.7 %</b>	<b>362.3 %</b>	<b>100.0 %</b>

## Side note: Google books



Create a **universal digital library** for the world.

Fictive project plan for digitizing books.

Currently approx. **10 M scanned** (2 trillion words)

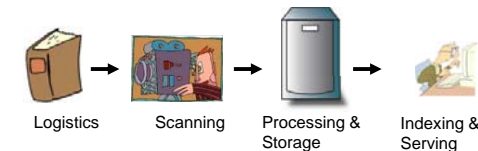
40 libraries, 25K partners

Number of books	30,000,000
Years of project	10
Books per year	3,000,000
Books per day	12,000
Pages per book	330
Pages per day	3,960,000
Image size per page	5
TBs a day	20
PBs per year	5
Pbs for project	50
Market cost per book	50
Cost of project at Market rate	1,500,000,000

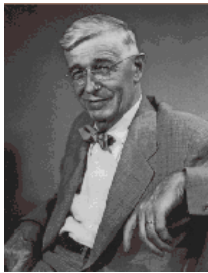


### L'IDEE FINE

La mort ? Elle est pour lui un accident, même un accident.  
— C'est qu'il se sent pas davantage concevoir la vie, dont la mort est une des propriétés nécessaires. La vie est, en somme, quelque éternellement linéaire, ordinairement ordonné dans une période de douze à quinze mille années d'espérance.  
— Et d'ailleurs...  
— Naturellement... Tout ce qui est accident est regrettable. Et accidentel, la vie a quelque chose d'un accident... qui s'est fait des fois.  
— Oui... Et dans cette courbe même, vie et mort... Est-ce et mort. La loi fondamentale est statistique. Point de vie sans mort ! c'est l'équation statistique.  
— Et c'est là que vous intervenez, monsieur Bismarck.  
— Pourquoi.  
— L'intelligence se comprend rien à



## Search as a principle & problem



"The difficulty seems to be, not so much that we publish unduly in view of the extent and variety of present day interests, but rather that **publication has been extended far beyond our present ability to make real use of the record**. The summation of human experience is being expanded at a prodigious rate, and the means we use for threading through the consequent maze to the momentarily important item is the same as was used in the days of square-rigged ships."

We live in a **search society** - belief that (almost) everything is known, we just have to find the information

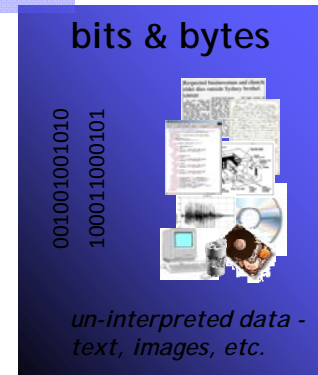
We **search for everything** - the right book, movie, car, house, vacation trip, bargain, partner, search engine etc.



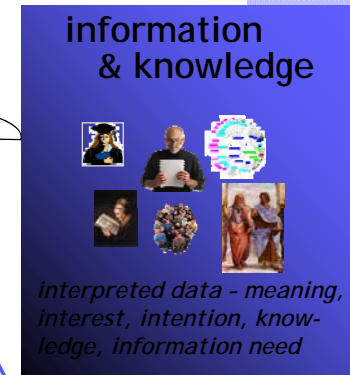
V. Bush. *As we may think*. Atlantic Monthly. 176 (1945). pp.101-108

## Machine learning in search

syntax



semanti



machine learning

interpretation

unsupervised learning & data mining:  
discover hidden regularities, generate semantically meaningful representations, predictive modeling, statistics

generalization

supervised learning:  
generalize from given examples, classification & recognition, emulate human experts

## 1. Text Categorization



## Document Annotations

- Categories as metadata: example, Reuters news stories

```
<code code="UK">
  <editdetail attribution="Reuters BIP Coding Group"
    action="confirmed" date="1996-08-20" />
</code>
<codes>
- <codes class="bip:topics:1.0">
- <code code="M13">
  <editdetail attribution="Reuters BIP Coding Group"
    action="confirmed" date="1996-08-20" />
</code>
- <code code="M132">
  <editdetail attribution="Reuters BIP Coding Group"
    action="confirmed" date="1996-08-20" />
</code>
- <code code="MCAT">
  <editdetail attribution="Reuters BIP Coding Group"
    action="confirmed" date="1996-08-20" />
</code>
</codes>
```

M13 = MONEY MARKETS

M132 = FOREX MARKETS

MCAT = MARKETS

# Text categorization & taxonomies

## Business Taxonomies



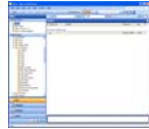
## Document Classification



## Patent Classification



## Email folders



## Web Directories



## Help Desks CRM



## Tasks:

- Assign documents to one of more pre-defined categories
- Route messages to an appropriate expert, employee, or department
- Automatically organize content into folders

## Types of texts:

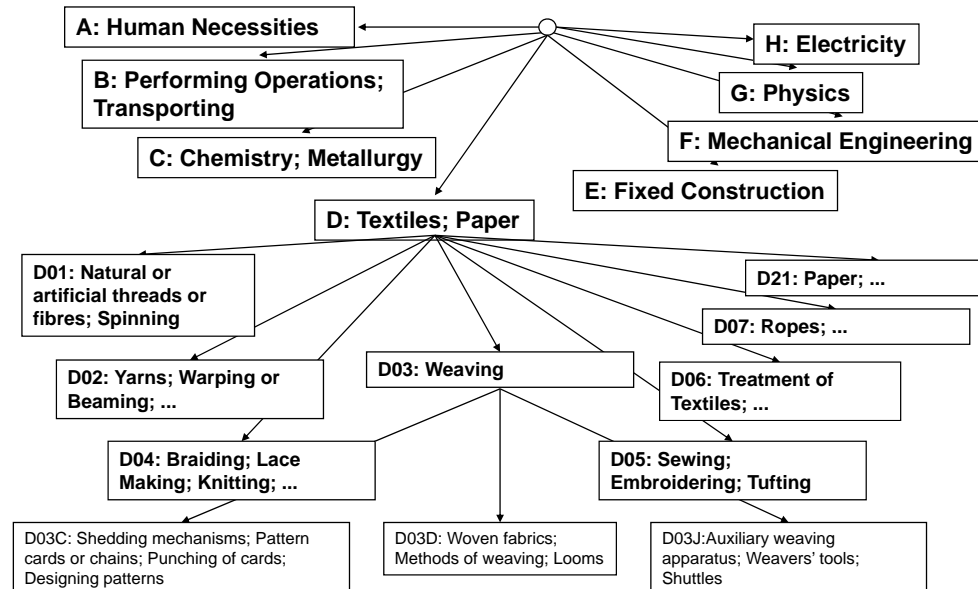
- text documents
- web pages, web sites
- messages, emails, SMS, chat transcripts
- passages & paragraphs, sentences

## Types of categories

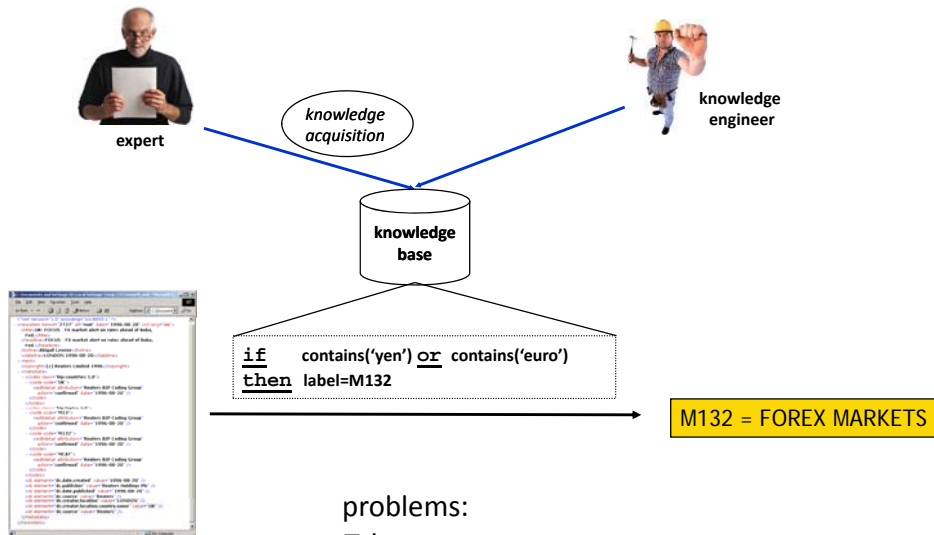
- topics, functions, genre, author, style, dichot (e.g. spam/nom-spam), industry vertical, sentiment, language

# taxonomies: international patent classification (IPC)

▶ IPC: section, class, subclass, group, subgroup ≈ 69,000



# Solution (?): Explicit knowledge elicitation



## problems:

- low coverage
- moderate accuracy
- elicitation is often difficult and time-consuming

# Solution (!): Example-based text categorization

## training examples

M132 = FOREX MARKETS



expert



training



learning machine

inductive inference

/\* some 'complicated algorithm' \*/

recall

M132 = FOREX MARKE



## Term document matrix & document vectors

D = document collection

W = lexicon/vocabulary

intelligence

$w_j$

Texas Instruments said it has developed the first 32-bit computer chip designed specifically for artificial intelligence applications [...]

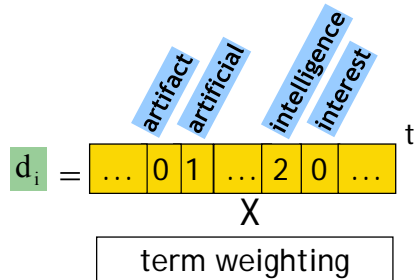
term document matrix

W

$w_1$  ...  $w_j$  ...  $w_j$

	$w_1$	...	$w_j$	...	$w_j$
$d_1$					
...			...		
$d_i$		...	$t f_{ij}$	...	
...			...		
$d_1$					

D



## Binary Classification

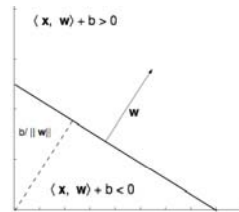
- Each document is encoded as a feature vector
- Predict whether document belongs to a given category or not.

Use linear classifier  $f: \mathbb{R}^d \rightarrow \{-1, 1\}$ ,  $f(\mathbf{x}) = \text{sign}(\langle \mathbf{w}, \mathbf{x} \rangle + b)$

Parameter

- Geometric view: separating hyper-planes
- Goal: minimize expected classification error

$$E[y \neq f(\mathbf{x})] = \int \frac{(1 - yf(\mathbf{x}))}{2} dP(\mathbf{x}, y)$$



- Given: training set of labeled examples

$$\{(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_m, y_m)\}$$

## 2. Supervised Classification

### Perceptron Learning Algorithm

- Invented in the late 1950ies
  - $\mathbf{w} \leftarrow 0, b \leftarrow 0$
  - repeat**
  - $errors \leftarrow 0$
  - /\* cycle through all training example*
  - for**  $i = 1, \dots, n$  **do**
  - if**  $\text{sign}(\langle \mathbf{w}, \mathbf{x}_i \rangle + b) \neq y_i$  **then**
  - $\mathbf{w} \leftarrow \mathbf{w} + y_i \mathbf{x}_i$
  - $b \leftarrow b + y_i$
  - $errors \leftarrow errors + 1$
  - end if**
  - end for**
  - until**  $errors = 0$
- Extremely simple, yet powerful (extensions)
- Discarded by Minsky & Papert 1960ies
- Re-discovered in the 1990ies
- Mistake driven** algorithm

## Novikoff's Theorem

- Functional margin of a data point with respect to classifier

$$\gamma_i \equiv y_i \langle \mathbf{w}, \mathbf{x}_i \rangle + b$$

(signed distance, if weight vector = unit length)

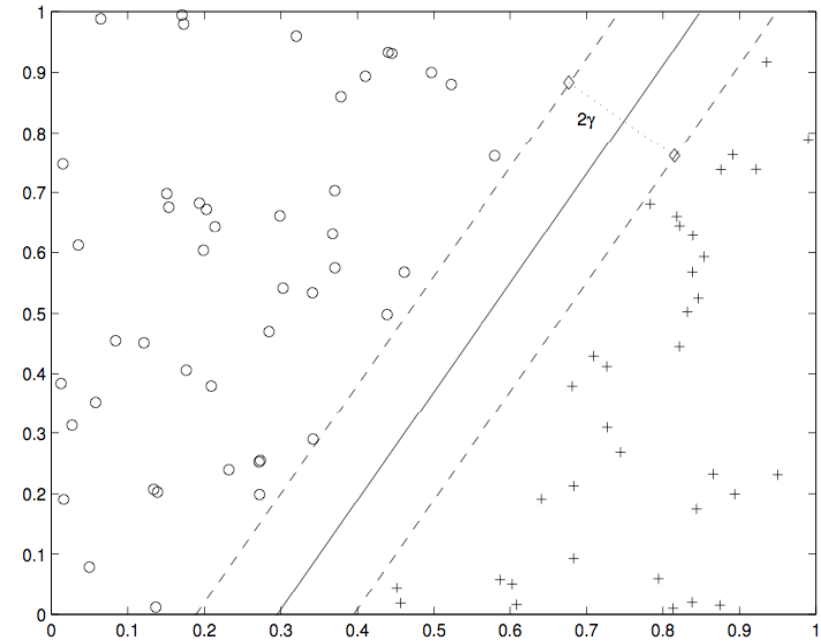
- Theorem:

Assume that there exists a weight vector  $\mathbf{w}^*$  with  $\|\mathbf{w}^*\| = 1$  such that  $\gamma_i = y_i \langle \mathbf{w}^*, \mathbf{x}_i \rangle \geq \gamma$  for all examples.

Then the perceptron will not make more than  $(R/\gamma)^2$  update steps.

(R is the radius of a data enclosing sphere)

## Separation Margin



## Novikoff's Theorem: Proof

- Lower Bound

$$\langle \mathbf{w}^{(t)}, \mathbf{w}^* \rangle = \langle \mathbf{w}^{(t-1)}, \mathbf{w}^* \rangle + y_i \langle \mathbf{x}_i, \mathbf{w}^* \rangle \geq \langle \mathbf{w}^{(t-1)}, \mathbf{w}^* \rangle + \gamma$$

$$\langle \mathbf{w}^{(t)}, \mathbf{w}^* \rangle \geq t\gamma$$

- Upper Bound

$$\|\mathbf{w}^{(t)}\|^2 = \|\mathbf{w}^{(t-1)}\|^2 + y_i^2 \|\mathbf{x}_i\|^2 + 2y_i \langle \mathbf{w}^{(t-1)}, \mathbf{x}_i \rangle$$

$$\leq \|\mathbf{w}^{(t-1)}\|^2 + \|\mathbf{x}_i\|^2 \leq \|\mathbf{w}^{(t-1)}\|^2 + R^2$$

$$\|\mathbf{w}^{(t)}\|^2 \leq tR^2$$

- Squeezing relations

$$\|\mathbf{w}^*\| \sqrt{t}R \geq \|\mathbf{w}^*\| \|\mathbf{w}^{(t)}\| \geq \langle \mathbf{w}^*, \mathbf{w}^{(t)} \rangle \geq t\gamma \implies t \leq R^2/\gamma^2$$

## Compression Bound

- Theorem:

For a fixed sample size  $m$  and  $d \leq m$ . Let  $\mathbf{X}$  denote a sample set of size  $m$  drawn i.i.d. according to some unknown probability distribution  $\mathbf{P}$ . Assume based on  $\mathbf{X}$  the perceptron algorithm converges after making mistakes on exactly  $d$  different examples. Then the probability that the generalization error of the obtained classifier is greater than  $\epsilon$  is at most

$$\binom{m}{d} (1 - \epsilon)^{m-d}$$

## Proof of compression bound

- The probability of a classifier with generalization error  $> \epsilon$  to classify  $n$  (i.i.d.) examples correctly is at most  $(1 - \epsilon)^n$ .
- Fix a subset of examples  $\mathbf{X}_d \subset \mathbf{X}$ . Consider potential solutions  $\mathbf{w}(\mathbf{X}_d)$  that classify  $\mathbf{X}$  correctly, but that perform updates only on elements of  $\mathbf{X}_d$ . The probability for such a solution to be  $\epsilon$ -bad is at most  $(1 - \epsilon)^{m-d}$ .
- There are  $\binom{m}{d}$  ways to select  $d$  examples from the  $m$ -sample  $\mathbf{X}$ , hence there are that many sets  $\mathbf{X}_d$  and corresponding  $\mathbf{w}(\mathbf{X}_d)$ .
- The perceptron solution is in one of the  $\mathbf{w}(\mathbf{X}_d)$  sets. Don't know which one, but can apply the union bound.

## Generalization Bound

- Generalization bound:

Theorem: With probability more than  $1 - \delta$  over random draws of the sample  $\mathbf{X}$  the following statement holds. If the perceptron algorithm converges by making mistakes on  $d$  examples, then the generalization error is less than

$$\frac{1}{m-d} \left[ \log \binom{m}{d} + \log m + \log \frac{1}{\delta} \right]$$

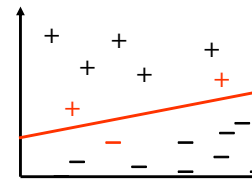
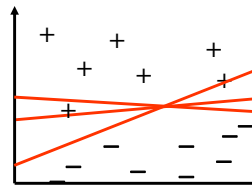
- The fewer mistakes are made in training, the better the guaranteed accuracy of the classifier.

## Margin Maximization (Support Vector Machines)

- Separation margin (and sparseness) crucial for perceptron learning
- Idea: explicitly **maximize separation margin**

$$(\mathbf{w}^*, b^*) = \underset{(\mathbf{w}, b), \|\mathbf{w}\|=1}{\operatorname{argmax}} \gamma$$

such that  $\forall i: y_i(\langle \mathbf{w}, \mathbf{x}_i \rangle + b) \geq \gamma$



- Reformulate as **quadratic program**

$$\begin{aligned} &\text{minimize} && \frac{1}{2} \|\mathbf{w}\|^2 \\ &\text{s.t.} && y_i(\langle \mathbf{w}, \mathbf{x}_i \rangle + b) \geq 1, \quad \forall 1 \leq i \leq n \end{aligned}$$

## support vector machines

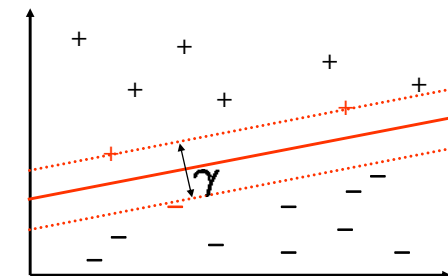
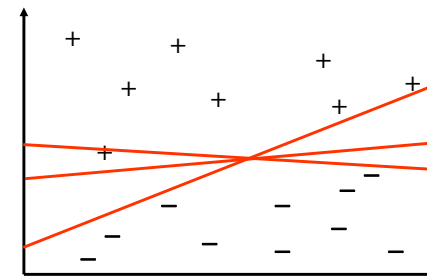
restriction to linear classifiers

$$f(\mathbf{x}) = \operatorname{sign}(\langle \boldsymbol{\theta}, \mathbf{x} \rangle + b)$$

0	0	1	0	4	4		
2	0	1	1	0	0		

tf-idf

maximum margin principle



# 1. Text Categorization (cont'd)



## Precision & Recall

	True label +1	True label -1
Predicted label +1	TRUE POSITIVE	FALSE POSITIVE
Predicted label -1	FALSE NEGATIVE	TRUE NEGATIVE
$\Sigma$	TOTAL POSITIVE	TOTAL NEGATIVE

Precision =

$$\frac{\text{true positives}}{\text{true positives} + \text{false positives}}$$

Recall =

$$\frac{\text{true positives}}{\text{true positives} + \text{false negatives}}$$

## Experimental Evaluation

- Text categorization results:

microaveraged precision/recall breakeven-point [0..100]	Reuters	WebKB	Ohsumed
Naive Bayes	72.3	82.0	62.4
Rocchio Algorithm	79.9	74.1	61.5
C4.5 Decision Tree	79.4	79.1	56.7
k-Nearest Neighbors	82.6	80.5	63.4
<b>SVM</b>	<b>87.5</b>	<b>90.3</b>	<b>71.6</b>

- Machine Learning award 2009: most influential paper from 1999 [ Thorsten Joachims, ICML 1999 ]
- Much follow-up research ...

## Practical Use Cases

### Google

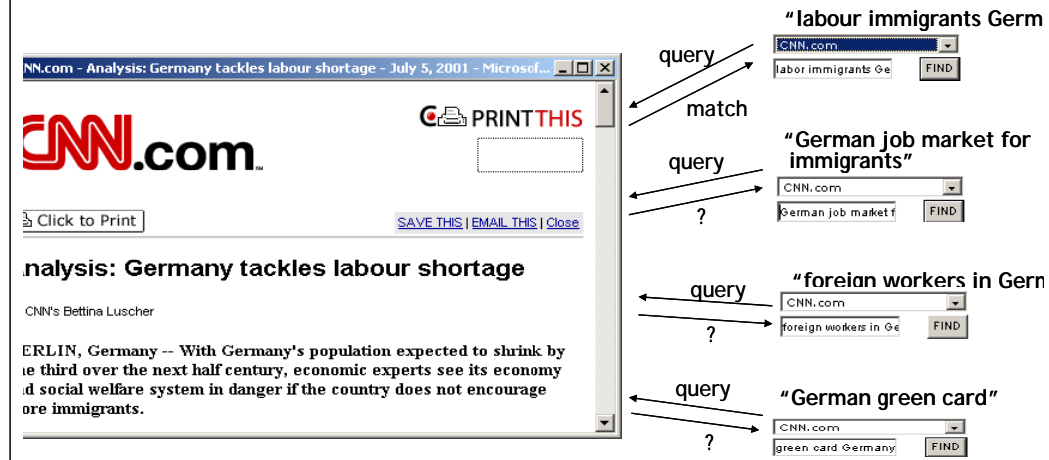
- label Web pages as child safe or not (for safe search)
- classifies billions of pages
- Many other features (other than text) used

### Recommind

- Map documents to corporate taxonomy
- MindServer classification
- uses SVM light package

### 3. Semantic Search

### Vocabulary mismatch problem



G. W. Furnas, T. K. Landauer, L. M. Gomez, S. T. Dumais, *The Vocabulary Problem in Human-System Communication: an Analysis and a Solution*. Bell Communications Research, 1987

### Search as statistical inference

document in bag-of-words representation



**China US trade relations**

Search

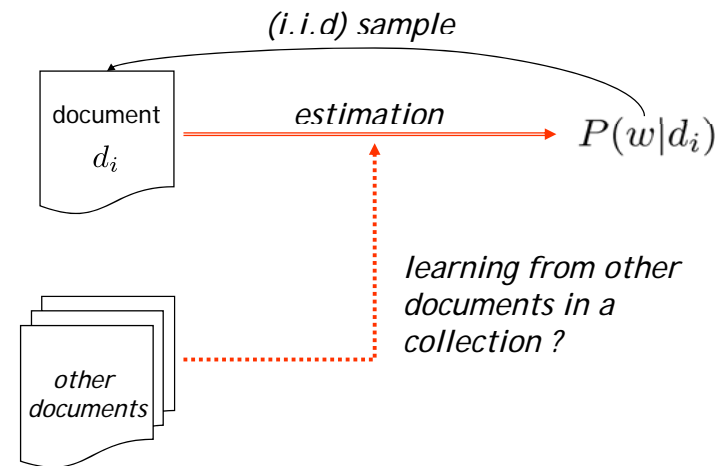
$P('China'|all\ other\ words)$

$P('trade'|all\ other\ words)$

How probable is it that terms like "China" or "trade" might occur?

automatically inferred key words can be added to enrich document index  
**document expansion**

### Estimation problem

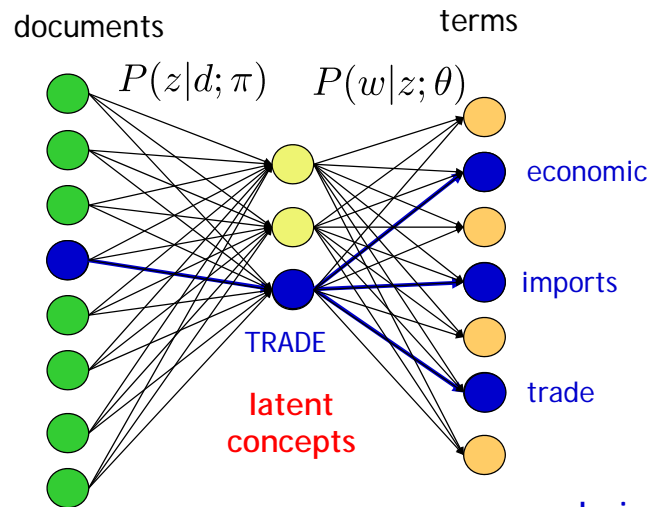


- crucial question:** In which way can the document collection be utilized to improve probability estimates?



# 4. Probabilistic Semantic Analysis

## Estimation via probabilistic LSA



concept expression probabilities are estimated based on all documents that are dealing with a concept.

“unmixing” of superimposed concepts is achieved by statistical learning algorithm.

**conclusion:** ⇒ no prior knowledge about concepts required, context and term co-occurrences are exploited

T. Hofmann. *Probabilistic Latent Semantic Analysis*. Uncertainty in Artificial Intelligence. UAI 1999.

## pLSA - latent variable model

structural modeling assumption (**mixture** model)

$$\hat{P}(w|d) = \sum_{z=1}^k P(w|z; \theta) P(z|d; \pi)$$

document language model

latent concepts or topics

document-specific mixture proportions

concept expression probabilities

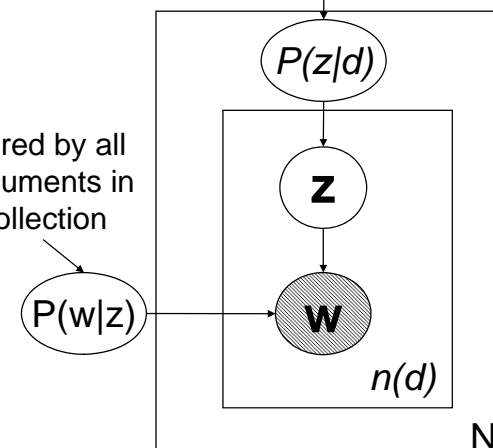
**model fitting**

## pLSA - graphical model

$$P(w|d) = \sum_z P(w|z) P(z|d)$$

shared by all words in a document

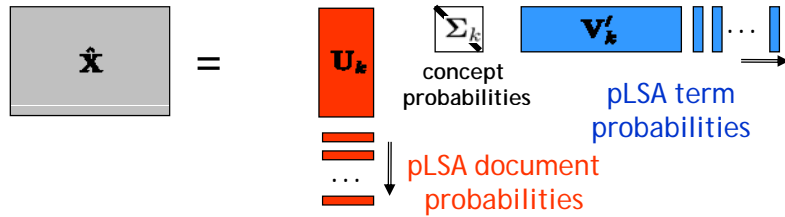
shared by all documents in collection



## pLSA: matrix decomposition

mixture model can be written as a **matrix factorization**  
equivalent symmetric (joint) model

$$\hat{P}(d, w) = \sum_{z=1}^k P(d|z) P(z) P(w|z) = P(d) \sum_z P(z) P(w|z)$$



contrast to LSA/SVD: **non-negativity** and **normalization** (intimate relation to non-negative matrix factorization)

D. D. Lee and H. S. Seung. *Algorithms for non-negative matrix factorization*. NIPS 13. pp. 556-562. 2001.

## pLSA via likelihood maximization

**log-likelihood**

$$L(\theta, \pi; n) = \sum_{d, w} n(d, w) \log \left[ \sum_z P(w|z; \theta) P(z|d; \pi) \right]$$

argmax  $(\hat{\theta}, \hat{\pi})$

observed word frequencies

$\hat{P}(w|d)$  predictive probability of pLSA mixture model

**goal**: find model parameters that maximize the log-likelihood, i.e. maximize the average predictive probability for observed word occurrences (**non-convex problem**)



*"The meaning of a word is its use in the language".*  
- Ludwig Wittgenstein. Philosophische Untersuchungen

## Expectation maximization algorithm

**E step**: posterior probability of latent variables ("concepts")

$$P(z|d, w) = \frac{P(z|d; \pi) P(w|z; \theta)}{\sum_z P(z|d; \pi) P(w|z; \theta)}$$

Probability that the occurrence of term  $w$  in document  $d$  can be "explained" by concept  $z$

**M step**: parameter estimation based on "completed" statistics

$$P(w|z; \theta) \propto \sum_d n(d, w) P(z|d, w)$$

how often is term  $w$  associated with concept  $z$ ?

$$P(z|d; \pi) \propto \sum_w n(d, w) P(z|d, w)$$

how often is document associated with concept

A.P. Dempster, N.M. Laird, and D.B. Rubin, *Maximum Likelihood from Incomplete Data via the EM Algorithm*, Journal of Statistical Society B. vol. 39 no. 1 pp. 1-38 1977

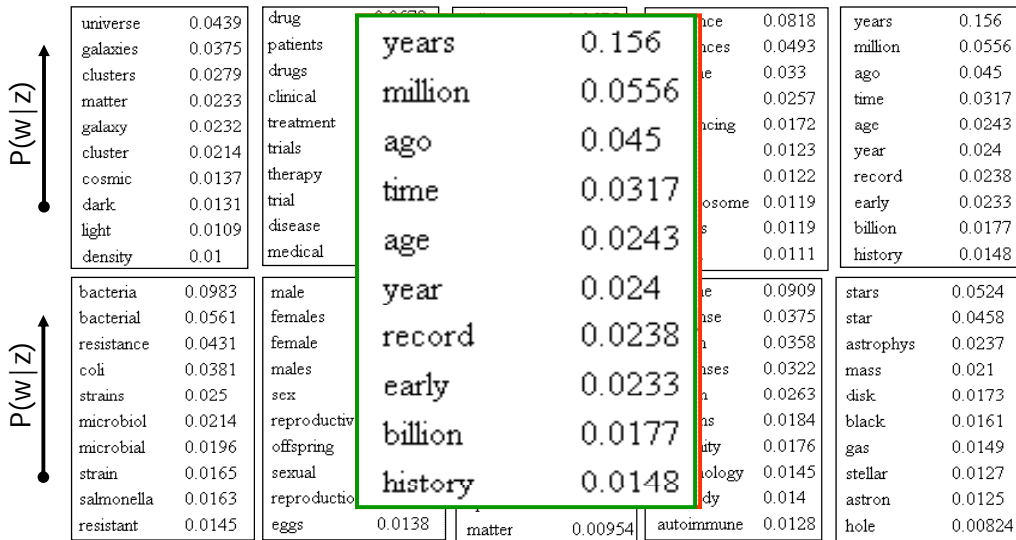
## Example

concepts (3 of 100) extracted from AP news

Concept 1		Concept 2		Concept 3	
securities	94.96324	ship	109.41212	india	91.74842
firm	88.74591	coast	93.70902	singh	50.34063
drexel	78.33697	guard	82.11109	militants	49.21986
investment	75.51504	sea	77.45868	gandhi	48.86809
bonds	64.23486	boat	75.97172	sikh	47.12099
sec	61.89292	fishing	65.41328	indian	44.29306
bond	61.39895	vessel	64.25243	peru	43.00298
junk	61.14784	tanker	62.55056	hindu	42.79652
milken	58.72266	spill	60.21822	lima	41.87559
firms	51.26381	exxon	58.35260	kashmir	40.01138
investors	48.80564	boats	54.92072	tamilnadu	39.54702
lynch	44.91865	waters	53.55938	killed	39.47202
insider	44.88536	valdez	51.53405	india's	39.25983
shearson	43.82692	alaska	48.63269	punjab	39.22486
boesky	43.74837	ships	46.95736	delhi	38.70990
lambert	40.77679	port	46.56804	temple	38.38197
merrill	40.14225	hazelwood	44.81608	shining	37.62768
brokerage	39.66526	vessels	43.80310	menem	35.42235
corporate	37.94985	ferry	42.79100	hindus	34.88001
burnham	36.86570	fishermen	41.65175	violence	33.87917

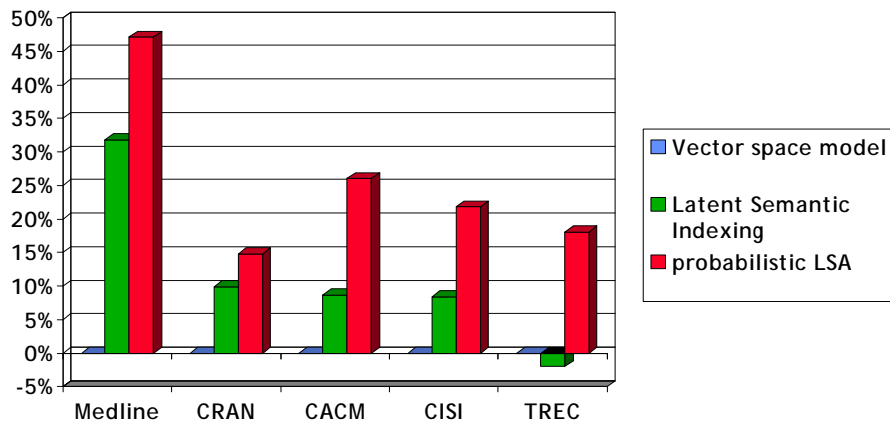
### Example

concepts (10 of 128) extracted from science magazine articles (12K)



### 3. Semantic Search (cont'd)

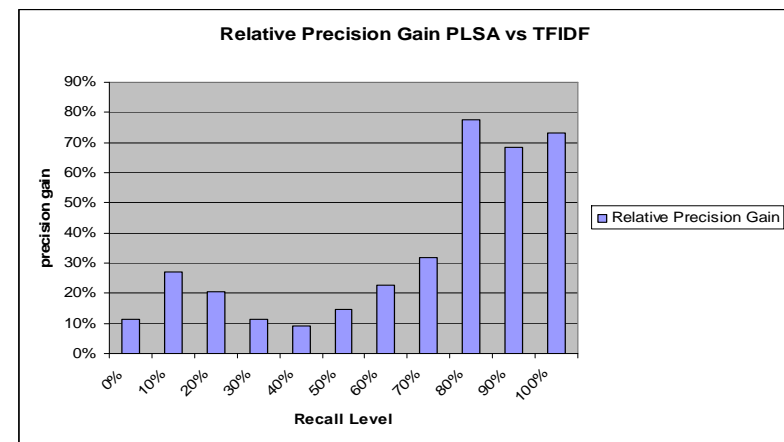
### Experimental evaluation



15-45% relative improvement gain in precision compared to SMART retrieval metric

### Experiments - TREC3 (AP collection)

comparison with TF-IDF metric (SMART) on TREC3



PLSA algorithms achieved a mean average precision (MAP) gain of 20%, in particular in the high recall range

# Practical Use Cases

## Google

- Somewhat similar model used to extract concepts from documents
- Used to improve search result ranking

## Recommind

- Heart of intelligent retrieval systems
- Many customers: Medline, law firms, enterprise search
- Allows to learn aspects of relevant semantics of domain purely based on co-occurrence statistics

# Med

The screenshot shows a Microsoft Internet Explorer browser window displaying the MedlinePlus website. The address bar shows a search query for "eye twitching". The page header includes the MedlinePlus logo and navigation links. The search results are displayed in two columns: "Search results found in:" and "Health Topics".

**Search results found in:**

- Health Topics
- Bell's Palsy (12)
- Eye Diseases (31)
- Vision Impairment and Blindness (11)
- Eye Injuries (10)
- Dystonia (7)
- Show all Health Topics
- Drug Information (477)
- Medical Encyclopedia (293)
- News (2)
- Other (0)

**Health Topics**

- Dystonia**  
Dystonia (National Library of Medicine)
- Benign Essential Blepharospasm (National Institute of Neurological Disorders and Stroke)
- Botulinum Toxin Injections: A Treatment for Muscle Spasms (American Academy of Family Physicians)
- Glossary of Terms (We Move)
- Blepharospasm (National Eye Institute)
- Dystoniae (National Institute of Neurological Disorders and Stroke)
- Dystonia: Diagnosis (We Move)

Page last updated: 01 October

# Med

The screenshot shows a Microsoft Internet Explorer browser window displaying the MedlinePlus website. The address bar shows a search query for "+eye +twitching". The page header includes the MedlinePlus logo and navigation links. The search results are displayed in two columns: "Search results found in:" and "Health Topics".

**Search results found in:**

- Health Topics
- Bell's Palsy (6)
- Eye Diseases (2)
- Dystonia (3)
- Facial Injuries and Disorders (2)
- Nutritional Support (2)
- Show all Health Topics
- Drug Information (84)
- Medical Encyclopedia (6)
- News (0)
- Other (0)

**Health Topics**

- Dystonia**  
Dystonia (National Library of Medicine)
- Benign Essential Blepharospasm (National Institute of Neurological Disorders and Stroke)
- Glossary of Terms (We Move)

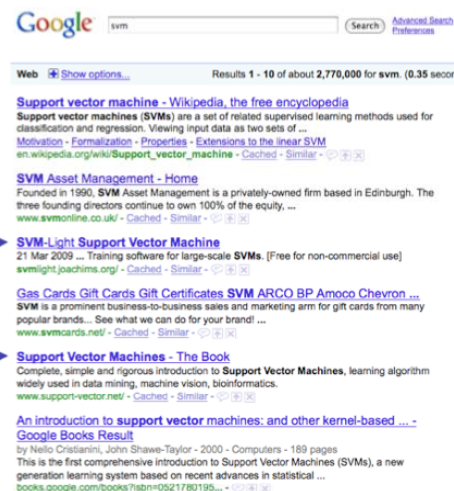
Page last updated: 01 October

## 5. Ranking

## Learning for Ranking: History

- ▶ Bollmann & Wong 1987 [BW87], Wong & Yao 1988 [WY88]
  - ▶ Acceptable ranking as one that respects known pairwise preferences
  - ▶ Perceptron algorithm to learn ranking function
- ▶ Fuhr 1989 [Fuh89]
  - ▶ Polynomial basis functions to map document-query representations to (known) relevance probabilities
  - ▶ Least squares regression
- ▶ Bartell et al. 1994 [BCB94]
  - ▶ Combination of different rankings (aka experts, meta search)
  - ▶ Linear expert score combination
  - ▶ Gutman's point alineation as a measure of rank correlation
  - ▶ Conjugate gradient descent optimization

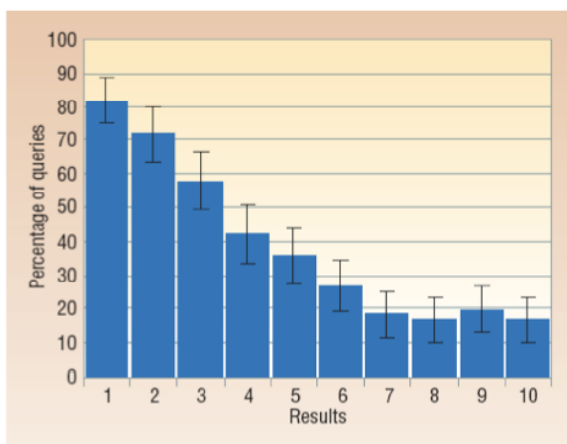
## Relative Relevance from Result Clicks



- ▶ Clicks do not imply absolute relevance judgments
- ▶ Scanning order: a click at rank  $k$  implies result is better than non-clicked on  $k' < k$
- ▶ Agnostic with regard to results below last click

- ▶ T. Joachims: Optimizing Search Engines Using Clickthrough Data [Joa02]

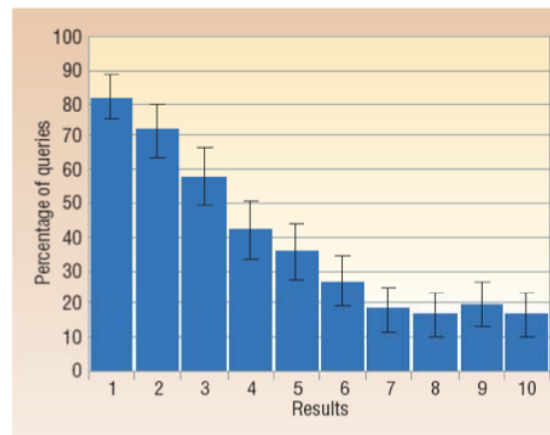
## What Users Look at: Eye Tracking Experiments



- ▶ % of queries where a user viewed result presented at particular rank
- ▶ Result beyond rank 3 examined < 50% of times
- ▶ Short attention span and skewed towards top positions

- ▶ Source: Joachims & Radlinski [JR07]

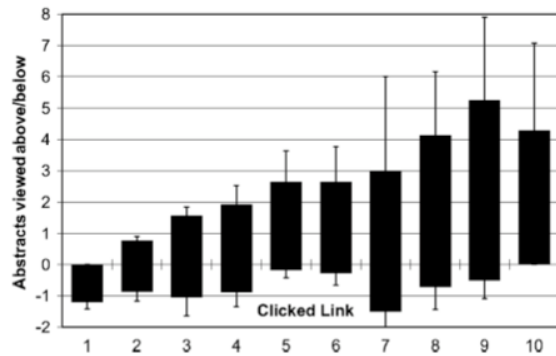
## Habitual Judgment Bias



- ▶ % of queries where a user viewed result presented at particular rank
- ▶ Result beyond rank 3 examined < 50% of times
- ▶ Short attention span and skewed towards top positions

- ▶ Source: Joachims & Radlinski [JR07]

## Scanning



- ▶ Mean number of snippets viewed before click on rank  $r$
- ▶ Only about 1 snippets examined following the clicked rank.
- ▶ # examined snippet increases with rank – not quite linearly (skips).

▶ Source: Granka, Joachims & Gay [GJG04]

## Attention Modeling: Findings

- ▶ Users only examine a **small portion** of the information displayed on a result page
- ▶ In result list view, the **top results** get dis-proportionately more attention
- ▶ Users typically **sequentially scan** the result list from top to bottom (with possible skips).
- ▶ **Acquired habits and experience** with search engines influence attention and click probability

## 6. Learning to Rank

### Relative Relevance Feedback from Result Clicks

- ▶ Extraction of **pairwise preferences**,  $u_i \prec u_j$  is a URL  $u_i$  is preferred over  $u_j$  with regard to a (fixed) query  $q$
- ▶ For a query  $q$  and a result ranking of URLs  $(u_1, u_2, u_3, \dots)$  with click variables  $c_i \in \{0, 1\}$ ,  $u_i \prec_q u_j$  if and only if  $i > j$  and  $c_i = 1 \wedge c_j = 0$ .
- ▶ Conservative preference extraction
- ▶ No absolute relevance assessment per query-URL pair

⇒ learning algorithms using pairwise preference training data

## Kendall's tau

- ▶ Kendall's  $\tau$ : similarity measure for rankings  $\pi, \pi' \in \mathcal{S}_n$
- ▶  $P =$  **concordant pairs** (i.e. URLs  $u_i$  and  $u_j$  with  $i = j$  ordered in the same manner by  $\pi$  and  $\pi'$ .)
- ▶  $Q =$  **discordant pairs**
- ▶ Definition

$$\tau(\pi, \pi') = \frac{P - Q}{P + Q} = 1 - \frac{2Q}{\binom{n}{2}}$$

- ▶ Example

$$\begin{aligned} \pi &= (1, 2, 3, 4, 5) \\ \pi' &= (3, 2, 1, 4, 5) \\ \tau(\pi, \pi') &= \frac{7 - 3}{7 + 3} = 0.4 \end{aligned}$$

## Kendall's tau

- ▶ Fulfills axioms of Kemeny & Snell
- ▶ In case of binary relevance, related to average precision:

$$AvPrec(\pi) = \frac{1}{R} \left[ Q + \binom{R+1}{2} \right]^{-1} \left( \sum_{i=1}^R \sqrt{i} \right)^2$$

where  $R$  is the number of relevant documents (cf. [Joa02])

- ▶ Learning goal: Minimize expected  $\tau$  over query/ranking pairs

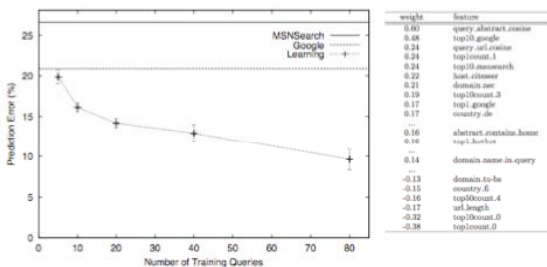
$$\mathbf{E}_P[\tau(f)] = \int \tau(\pi^*, \pi_{f(q)}) dP(q, \pi^*)$$

## SVM Ranking for Pairwise Preferences

- ▶ Basic idea: enforce a **separation margin** on each known preference pair
- ▶ Formally (with slack variables):

$$\langle \mathbf{w}, \Phi(q, u_i) - \Phi(q, u_j) \rangle \geq 1 - \xi_{i,j,q}, \quad \forall i, j : u_i \prec_q u_j$$

- ▶ For given  $q$ , URLs  $u$  can be ranked according to  $\langle \mathbf{w}, \Phi(q, u) \rangle$ .



- ▶ Metasearch engine
- ▶ Example features
- ▶ Source: [Joa02]

## Features used for ranking

What features should be used in the  $\Phi$  function?

- should describe the match between a document  $d$  and a query  $q$
- examples
  - number of words shared by query and document
  - number of shared words inside certain HTML tags
  - cosine similarity between query and document title or abstract
  - page rank of document  $d$
  - rank of  $d$  in the result list of  $q$  for some search engine (e.g. within top10, within top50, etc.)
  - properties of the URL (contains tilde, length, etc.)
  - ...

## Learned Ranking

Comparison	more clicks on learned	less clicks on learned	tie (with clicks)	no clicks	total
Learned vs. Google	29	13	27	19	88
Learned vs. MSNSearch	18	4	7	11	40
Learned vs. Toprank	21	9	11	11	52

weight	feature
0.60	query_abstract_cosine
0.48	top10_google
0.24	query_url_cosine
0.24	top1count_1
0.24	top10_msnsearch
0.22	host_citeseer
0.21	domain_nec
0.19	top10count_3
0.17	top1_google
0.17	country_de
...	
0.16	abstract_contains_home
0.16	top1_hotbot
...	
0.14	domain_name_in_query
...	
-0.13	domain_tu-bs
-0.15	country_fi
-0.16	top50count_4
-0.17	url_length
-0.32	top10count_0
-0.38	top1count_0

- ▶ Features have been (roughly) hand designed
- ▶ Numbers indicate weights learned by ranking SVM

## Applications

- How can the learning from clickthrough data approach be applied?
  - clickthrough can not be used immediately to improve search results for a specific query
  - preferences can be aggregated over the **whole user population** to **self-optimize a parameterized ranking function**
  - optimization can also be performed for **specific groups of users** (e.g. users from the same country) to construct **adaptive and personalized ranking functions**
- In particular:
  - **meta-search engine**: combine results from different search engines (e.g. parameterized ranking function corresponds to combination of search results)

## 7. Summary

## Machine Learning for Search

### Text categorization:

Experts label documents, computers learn to generalize to new documents -> scalability & automation

### Semantic search:

Statistical models learned from document corpus help bridge the semantic gap in search -> more relevant search results

### Learning to rank:

Users provide implicit feedback through clicks that help improve the result ranking.

Many more, related applications ... Many more methods ...

The future: **intelligent Web**

- use of social intelligence and machine learning.